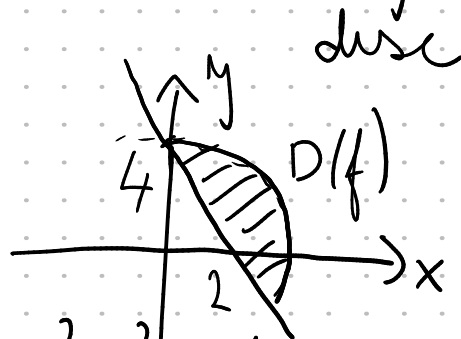


$$d) \quad 2x + y - 4 \geq 0 \quad \wedge \quad 16 - x^2 - y^2 \geq 0$$

$$y \geq 4 - 2x \quad \wedge \quad x^2 + y^2 \leq 16$$

$$\partial: \quad y = 4 - 2x$$

--- line



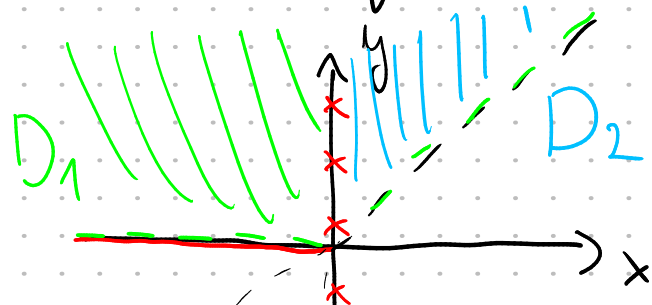
$$D(f) = \{ [x, y] \in \mathbb{R}^2; x^2 + y^2 \leq 16 \wedge y \geq 4 - 2x \}$$

$$e) \quad 1. \quad x^2 y > 0$$

$$x \neq 0 \vee y > 0$$

$$2. \quad y - x > 0$$

$$\wedge \quad y > x$$



$$D(f) = D_1 \cup D_2$$

$$D_1 = \{ [x, y] \in \mathbb{R}^2; x < 0 \wedge y > 0 \}$$

$$D_2 = \{ [x, y] \in \mathbb{R}^2; x > 0 \wedge y > x \}$$

$$D(f) = \{ [x, y] \in \mathbb{R}^2; x \neq 0 \wedge y > 0 \wedge y > x \}$$

$$f) = \arcsin g$$

$$g = \frac{y-1}{x}$$

$$-1 \leq g \leq 1$$

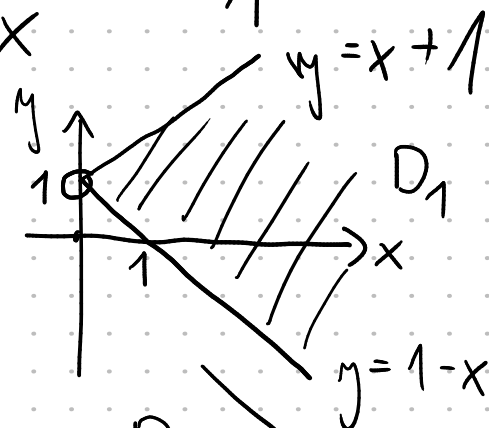
$$\wedge \boxed{x \neq 0}$$

$$-1 \leq \frac{y-1}{x} \leq 1$$

$$\boxed{x > 0}$$

$$-x \leq y-1 \leq x$$

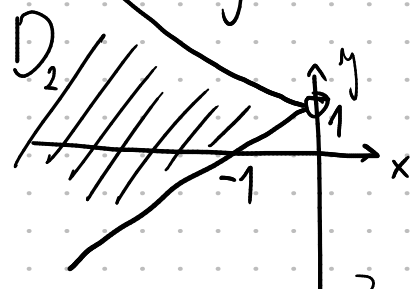
$$1-x \leq y \leq x+1$$



$$\boxed{x < 0}$$

$$-x \geq y-1 \geq x$$

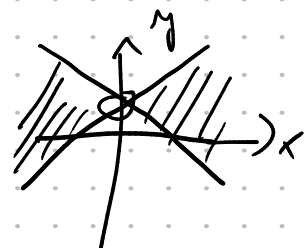
$$1-x \geq y \geq 1+x$$



$$D_1 = \{ [x, y] \in \mathbb{R}^2 ; 1-x \leq y \leq x+1 \wedge x > 0 \}$$

$$D_2 = \{ \text{---} \text{---} \text{---} ; 1-x \geq y \geq x+1 \wedge x < 0 \}$$

$$D(f) = \underline{\underline{D_1 \cup D_2}}$$

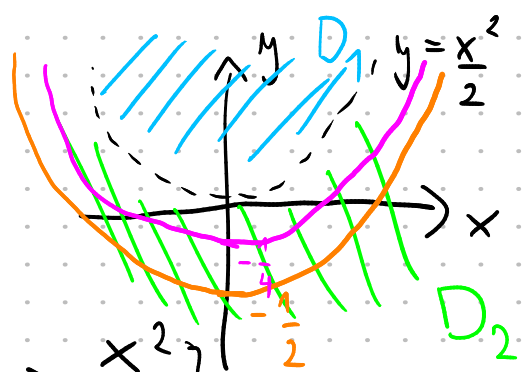


$$3a) \quad x^2 - 2y \neq 0$$

$$y \neq \frac{x^2}{2}$$

$$D_1 = \left\{ [x, y] \in \mathbb{R}^2 ; y > \frac{x^2}{2} \right\}$$

$$D_2 = \left\{ [x, y] \in \mathbb{R}^2 ; y < \frac{x^2}{2} \right\}$$



$$D(f) = \underline{\underline{D_1 \cup D_2}}$$

iso-curve

$$f(x, y) = 1$$

$$z = 1$$

$$\frac{1}{x^2 - 2y} = 1$$

$$1 = x^2 - 2y$$

$$y = \frac{x^2 - 1}{2} = \frac{x^2}{2} - \frac{1}{2}$$

$k=2$ :

$$f(x, y) = 2$$

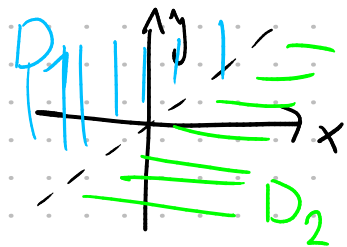
$$\frac{1}{x^2 - 2y} = 2$$

$$1 = 2x^2 - 4y$$

$$y = \frac{1}{4}(2x^2 - 1) = \frac{x^2}{2} - \frac{1}{4}$$

$$3b) f(x, y) = e^{1/(x-y)}$$

$$x-y \neq 0 \Rightarrow x \neq y$$



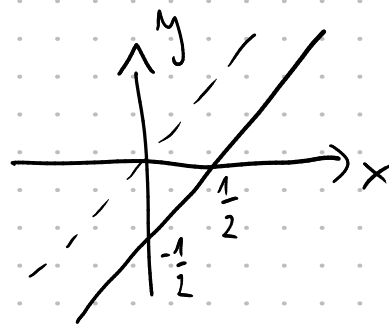
$$D(f) = \{[x, y] \in \mathbb{R}^2; x \neq y\} = D_1 \cup D_2$$

iso-curve:  $f(x, y) = e^2$

$$e^{1/(x-y)} = e^2$$

$$\frac{1}{x-y} = 2$$

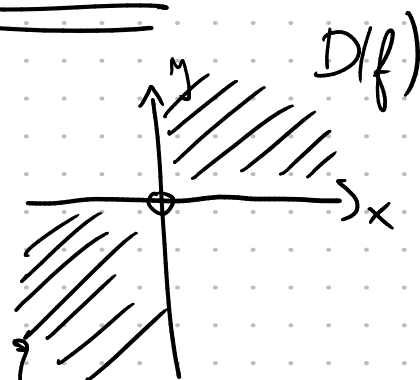
$$\frac{1}{2} = x - y \Rightarrow y = x - \frac{1}{2}$$



c)  $xy > 0$

$$x > 0 \wedge y > 0$$

$$x < 0 \wedge y < 0$$



$$D_1 = \{[x, y] \in \mathbb{R}^2; x > 0 \wedge y > 0\}$$

$$D_2 = \{[x, y] \in \mathbb{R}^2; x < 0 \wedge y < 0\}$$

$$D(f) = D_1 \cup D_2$$

iso-curve:  $f(x, y) = 0$

$$\frac{\sin xy}{\sqrt{xy}} = 0 \Rightarrow \sin xy = 0$$

$$\Rightarrow \sin xy = 0$$

$$xy = 2\pi; \forall k \in \mathbb{Z}^+$$

$$y = \frac{2\pi}{x}$$

